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BRIEF REPORT

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Fast and effective: Intuitive processes in complex decisions

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10 Abstract

Is it possible to carry out complex multi-attribute decisions (which require an estimation of the weighted average) intuitively, 11 12without resorting to simplifying heuristics? Over the course of 600 trials, 26 participants had to choose the better-suiting jobcandidate, a task requiring comparison of two alternatives over three/four/five dimensions with specified importance weights, 1314with a time constraint forcing intuitive decisions. Participants performed the task fast (mean reaction time $(RT) \sim 1.5$ s) and with high accuracy (~86%). The participants were classified as users of one of three strategies: Weighted Additive Utility (WADD), 15Equal Weight rule and Take-The-Best heuristic (TTB). Fifty-nine percent of the participants were classified as users of the 1617compensatory WADD strategy and 29% as users of the non-compensatory TTB. Moreover, the WADD users achieved higher task accuracy without showing time costs. The results provide support for the existence of an automatic compensatory mecha-18 19nism in weighted average estimations.

20 Keywords Decision making · Weighted average · Compensatory process · Take-the-best

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22 Introduction

Complex decisions, such as selecting a job candidate or a 23vacation package, are among the most demanding and chal-24lenging human activities. A major cause of this challenge is 2526the presence of trade-offs between attributes (e.g., intelligence vs. motivation for job candidates) that are difficult to compare. 27While a normative theory, based on weighted additive utility 28(WADD), was developed by early decision theorists (Keeney 2930 & Raiffa, 1976), a widely accepted view considers that the computations required for the normative WADD algorithm 31are too complex for online human decisions (not assisted by 32 offline calculations or external aids). Accordingly, it is often 33

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¹ School of Psychological Sciences and Sagol School of Neuroscience, Tel-Aviv University, Haim Levanon 55, PO Box 39040, Tel-Aviv, Israel assumed that when faced with such decisions, humans typi-34cally resort to a number of simplifying non-compensatory 35heuristics, such as Take-the-Best (TTB), according to which 36 one chooses on the basis of the most important attribute (in 37 case of a tie, the second most important attribute is considered; 38 Gigerenzer & Goldstein, 1996, 1999; Payne, Bettman, & 39 Johnson, 1993; but see Newell, 2005, for a critique of this 40 approach and suggestions of formal models of ecological 41 rationality). Such heuristics simplify the decision algorithm, 42 by replacing the compensatory processes - in which all the 43 attributes are weighted into the decision - with a non-44 compensatory one, in which only a small subset of the attri-45butes is taken into account (Dieckmann & Rieskamp, 2007; 46Gigerenzer & Goldstein, 1999; Tversky, 1969, 1972). 47

Recent research has challenged the assumption that com-48pensatory strategies are too complex and thus beyond daily 49decision-making ability. First, numerous studies in the domain 50of probabilistic inference with binary cues have shown that 51even when environments are designed to promote the use of 52TTB heuristic, a significant proportion of participants do not 53"take the best" (e.g., Bröder, 2000; Lee & Cummins, 2004; 54Newell & Shanks, 2003). Second, more recent experimental 55work has demonstrated that most participants make probabi-56listic inferences based on multiple cues in a compensatory yet 57rapid and automatic manner (Glöckner & Betsch, 2008, 2012; 58Glöckner, Hilbig, & Jekel, 2014). Other research has 59

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60 manipulated time pressure, confirming the presence of com-61 pensatory strategies with a 3-s response-deadline and, for 62 some participants, even for a strict deadline of 750 ms (Oh 63 et al., 2016).

64 A mechanistic account of such an automatic vet compensatory decision process was proposed by Glöckner and col-65 66 leagues in the form of the PCS model (Glöckner et al., 2014). PCS is a connectionist, accumulator-type model, that inte-67 grates (using a parallel architecture) differences in weighted 68 evidence (Δ WA) between the alternatives and predicts slower 69 reaction times (RTs) for decisions with smaller ΔWA 70(Glöckner & Betsch, 2008, 2012; see also Roe, Busemeyer, 71& Townsend, 2001 for a Decision-Field-Theory model of 72multi-attribute decisions). 73

In this paper we demonstrate an ability to make complex 74 decisions using compensatory, rapid, and automatic mecha-7576nisms in a different domain: multi-attribute decision-making based on numerical (non-binary) attributes. Such decisions 77 78normatively require a weighted averaging computation, tradi-79 tionally associated with analytical processes. Moreover, multiattribute decisions with non-binary attributes have received 80 less attention in recent research (see Russo & Dosher, 1983 81 82 and Tversky, 1969 for some older studies) and they differ from binary cue decisions in a number of important aspects (prob-83 lem-space is virtually infinite and precludes the use of simpli-84 85 fying strategies, such as memorizing or counting). Therefore, if rapid and compensatory (WADD) strategies can be deployed 86 in this domain, this would provide support for the impressive 87 power of the intuitive decision-maker. 88

Recent research has shown that an important precursor of
WADD – numerical averaging – can be estimated in a relatively precise and yet automatic manner (Brezis, Bronfman,
Jacoby, Lavidor, & Usher, 2016; Brezis, Bronfman, &
Usher, 2015; Rusou, Zakay, & Usher, 2017). Here we set to
test whether this ability extends to weighted averaging, by
employing a job selection multi-attribute decision task.

96 Experiment

97 Participants were asked to take the role of a job interviewer who chooses one of two candidates based on the candidates' 98abilities on several attributes and their relative importance. We 99 100varied (in blocks) the number of attributes (three/four/five), and we presented a large set of decision problems with ran-101102 domized values (see Methods). This design allows us to contrast decision strategies within each participant using choices 103and RTs. While the TTB heuristic predicts slower decisions in 104cases there is a tie on the most important attribute, PCS (or 105other accumulator models) predicts decision times that in-106107 crease with lower ΔWA . Another central question of interest is whether the deployment of compensatory strategies results 108in improved task performance. 109

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Participants

Method

Twenty-six students from Tel-Aviv University (14 females,112age: 19–31, M=24.7) participated in the experiment, in ex-113change for course credit and payment that was dependent on114performance. On average, participants received 30 NIS (~7.5115USD). The sample size was set at 26 with each subject tested116in three tasks, allowing for 78 (26 × 3) classifications in total117to be made (see Strategy Classifications118

Materials

Each decision was presented in a table-format (see Table 1). 120Three jobs were presented, with three, four, and five attributes, 121 respectively. Each job specified the attributes' importance (i.e., 122weight; see Table 1). When the job had three attributes, the 123specified importance-weights were 3, 2, and 1 (i.e., the most 124important attribute was three times more important than the 125least important attribute), for the four-attribute job they were 1264, 3, 2, and 1, and for the five-attribute job 5, 4, 3, 2, and 1. 127The values the candidates received in each trial were generat-128ed randomly, as random integers between 1 (poor) and 9 (ex-129cellent; from a uniform distribution; if the resulting weighted 130average for the two candidates was the same, the ratings were 131generated anew). 132

A time limit for providing an answer was imposed, in order 133to encourage participants to rely on their intuitive mind-set 134and not explicitly compute weighted averages (Horstmann, 135Hausmann, & Ryf, 2010). The time limit increased with the 136number of attributes that had to be considered to make sure 137that all the information can be encoded. The time limits were 1383 s for the 3-attributes, 4 s for the 4-attributes, and 5 s for the 5-139attribute jobs. As we report below, however, the time con-140straints did not affect the actual decision times. 141

Procedure

Participants completed 600 trials overall, with three 143blocks of 200 trials for each job (3, 4, or 5 attributes). 144On each trial, a choice problem (see Table 1) was pre-145sented until the participant entered a decision by using 146the keyboard. Visual feedback (correct/incorrect) was 147given after each trial, based on the weighted averages. 148Feedback was also given on the number of correct trials 149the participant accumulated, which was translated to 150monetary reward at the end of the experiment. Once the 151time limit expired, the trial ended, and the visual feed-152back, ("too slow," was presented. The whole procedure 153took approximately 60 min (see Supplementary Material 154for details). 155

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t1.1 **Table 1** Example of a trial in which the job had four attributes, with weights of 4, 3, 2, and 1. Here candidate A had the higher weighted average (5.2 vs. 4.3 for candidate B) and so she should be selected for the job, while candidate B should be selected according to *TTB* heuristic

t1.2		А	В
t1.3	Intelligence – 4	3	3
t1.4	Work Ethic – 3	5	7
t1.5	Easy to Work With -2	9	4
t1.6	Creativity - 1	7	2

156 **Results**

157 Group analyses

158 Accuracy

159To test effects of difficulty and task practice (defined across 160 four chunks of 50-trial sub-blocks) on task accuracy, a repeated-measures ANOVA was carried out, with number of 161162attributes (three/four/five) and sub-block as within-subject factors. As shown in Fig. 1 (solid lines), there was a main 163effect of difficulty (F(2,50)=37.39, p<.001). As the number 164of attributes increased accuracy dropped from 90% for the 165166 three attributes to 86% for four attributes and 84% for five attributes. No main effect of sub-block emerged 167(F(3,75)=1.16, p=.329), indicating that extensive learning is 168not necessary. For each number of attributes, the task-169accuracy was higher than a bound obtained from an error-170171less version of the TTB heuristic (dashed lines), F(1,25)=74.29, p < .001.172

173 Reaction times

174 Mean RT and the average number of trials (out of 200) in 175 which the time limit was missed are given in Table 2.

176A repeated-measures ANOVA, with number of attributes (three, four, five) as within-subject factor, revealed no effect of 177178number of attributes, F(1.25, 31.23)=0.056, p=.865. Thus, 179although the task's difficulty increased and more information had to be considered, participants did not require more time. 180The number of trials in which the time limit was missed was 181182only 0.6% of all trials and the average decision time was of 183around 1.5 s (see also Glöckner & Betsch, 2008, for similar results). 184

We also examined the correlation between RT and task accuracy. For each participant, we calculated the correlations between RT and accuracy, across all trials, separately for each number of attributes. The resulting mean correlations were negative, as predicted by the automatic *WADD* mechanism: r = -0.199 for three attributes, r = -0.203 for four attributes and r = -0.172 for five attributes. Interestingly, the negative 201

correlations between accuracy and RT remained even after 192controlling for the trials' difficulty: the partial correlation be-193tween RT and accuracy remained negative: r = -0.102 for three 194 attributes, r = -0.084 for four attributes, and r = -0.062 for five 195attributes. While these partial correlations are small, they are 196 all significantly different from 0 (all p's<.05, tested using a 197bootstrap procedure with 10,000 resamples) and in the same 198 direction, suggesting that taking longer to decide reduces 199accuracy. 200

Strategy classifications

We next examined individual differences in decision strate-202gies. We tested three potential strategies that participants could 203 use when performing the task: the weighted average WADD, 204TTB, and the Equal Weights rule combined with the TTB 205heuristic (EQW-TTB). According to the EQW-TTB strategy, 206 one chooses the alternative for which the non-weighted aver-207age is highest (i.e., the subjects average the values but ignore 208the importance weights). In cases where the non-weighted 209average for both alternatives is the same, participants choose 210according to the TTB heuristic, thus its name – EQW-TTB.¹ 211We start using a simplified "trembling-hand" approach 212(Bröder, 2010), according to which the subject has a probabil-213ity p to mistakenly report an alternative not predicted by the 214choice strategy. We use this approach in order to obtain an 215upper bound on the proportion of TTB use (we defer to the 216computational section, where we examine a more refined type 217of strategy-classifications allowing probabilistic errors and 218strategy mixtures). 219

The classifications were done separately for three/four/five 220attributes to test whether increased difficulty leads to more 221reliance on non-normative strategies. To classify the partici-222pants based on the three strategies - WADD, TTB, and EQW-223TTB – we computed the probability of the data (200 choices) 224 for each strategy and we selected the strategy that has the 225highest probability; see Supplementary Material for details 226of the classification procedure. The classification results are 227shown in Table 3 (see Table S1 in Supplementary Material for 228individual classifications and Tables S2, S3, and S4 for the 229normalized probabilities of the three strategies); 82% of the 230classifications (64 out of 78) are associated with normalized 231probability larger than .99, and 88% (69 out of 78) with a 232probability larger than .90. 233

As shown in Table 3, the majority of classifications (46 out of 78 in total, \sim 59%) belong to the compensatory (normative) 235 *WADD* strategy and another 8% (six in total) were a less optimal but still compensatory *EQW-TTB* strategy. Only 29% of 237 the classifications (23 in total) fell into the *non-compensatory* 238

¹ We also tested a less restrictive *Take-Two* heuristics (Dieckmann & Rieskamp, 2007), but none of the data sets were classified to this strategy and therefore we do not include it in Table 3.



Fig. 1 Task-accuracy. Solid-lines: accuracy as a function of the number of attributes and of trial-number (in 50-trial blocks). Dashed lines: theoretical performance of *TTB* heuristic. Error bars represent within-subject standard errors (Cousineau, 2005)

239*TTB* category. The amount of *WADD* classifications did not240vary with the number of attributes. A summary of participants'241accuracy as a function of strategy is shown in Fig. S1 (see242Supplementary Material). We find that users of the *WADD*243strategy had higher accuracy than *TTB* users, t(67)=3.08,244p=.003. As reported in the Supplementary Material, this is245not due to a speed-accuracy tradeoff.

246 Attributes' weights

Using logistic regression, we computed the subjective weights 247248each participant gave to each of the attributes. Figure 2 shows these subjective weights for the three strategy subgroups (see 249Fig. S2 in the Supplementary Material for the group weights). 250251These weights indicate that WADD users are better calibrated 252with the objective weights, the results of the TTB users show a strong overestimation of the most important attribute, 253254confirming their reliance on a single dimension. A repeated-255measures ANOVA on the attributes' weights of users of the TTB and WADD strategies revealed an interaction between the 256strategy used and the attributes' weights, for every number of 257attributes – for three attributes: F(2,42)=21.36, p<.001, for 258four attributes: F(3,63)=13.93, p<.001, and for five attributes: 259260F(4,92)=15.40, p<.001. The EQW-TTB users showed the flat-261test curves, consistent with the equality of weights character-262izing this strategy.

t2.1 **Table 2** Mean reaction time (RT) (standard deviations in parentheses) and average number of trials in which the time limit was missed (out of 200), for each number of attributes

t2.2		Three attributes	Four attributes	Five attributes
t2.3 t2.4	Mean-RT (SD) Number of trials exceeding deadline	1577 (512) 0.85	1593 (501) 1.27	1565 (519) 1.50

Reaction times: strategies and correlation with accuracy 263

The WADD and the TTB strategies differ in their predic-264tions concerning RT (Glöckner & Betsch, 2008). While 265according to TTB the RT should depend on whether there 266is a tie on the most important dimension, according to 267WADD the RT should depend on the absolute difference 268in the alternatives' weighted averages (Δ WA). To test this 269prediction, we applied to the log-RT-data of each partici-270pant (we used log-RT in order to normalize the otherwise 271skewed values in the RT-distribution that may involve 272outliers; see also Glöckner & Betsch, 2008) a multiple 273linear regression with two factors: (i) ΔWA , (ii) a binary 274predictor of a tie on the most important dimension (i.e., 275the most important attribute; see Table 1 for an example 276on which the tie variable equals 1 and $\Delta WA=0.9$). We 277compared the standardized regression coefficients for the 278participants who were classified as WADD users and those 279classified as TTB users. As predicted, the difficulty coef-280ficient was stronger for the WADD users (M = -0.43, SD =2810.12) compared with the TTB users (M = -0.32, SD =282 0.12; t(67)=3.56, p<.001; Fig. 3, left), while the tie coef-283ficient was higher in magnitude for the TTB users (M =2840.06, SD = 0.14) compared with the WADD users (M = -2850.02, SD = 0.09; t(31.8)=2.31, p=.027; Fig. 3, right). 286 Unlike for the TTB users, for the WADD users the tie-287coefficient was not significantly different from zero. 288

Computational-models of strategy choice:289beyond the trembling hand290

While the trembling-hand classifications appear to have some291validity, as they are supported by differences in subjective292weights (Fig. 2) and in RTs (Fig. 3), there are a number of293reasons to suspect that these classifications are a simplification294and that the participants vary in a more continual, non-dichot-295omous, manner. First, the weights are subject to individual296

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t3.1 **Table 3** Number of participants classified as users of each one of the three strategies (*WADD*, *TTB*, *EQW-TTB*) as a function of the number of attributes

Number of attributes		
Three	Four	Five
15	14	17
7	9	7
3	2	1
1	1	1
	Number of a Three 15 7 3 1	Number of attributesThreeFour1514793211

 $W\!ADD/TTB*$ represents cases in which these two strategies had equal probabilities

297 variability even within a strategy group, indicating continuity 298rather than dichotomous strategies. Second, even for partici-299pants classified as TTB, we obtain a WADD component in the 300 RT-regression (Fig. 3). Finally, as recently discussed by Hilbig 301 and Moshagen (2014), the trembling-hand type of error is not 302 well matched with the natural assumptions of a WADD model, according to which choice-problems with lower $\Delta W\!A$ are ex-303 pected to have more errors. In order to extend the strategy 304classification to address these issues, we examined a number 305306 of computational models and carried out model-comparison 307 using the aggregate Akaike Information Criterion (AIC; Akaike, 1973). As there are only six EOW classifications in 308 our data (out of 78), we discard these and focus on contrasting 309 310 between WADD and TTB.

Three new models were examined: (i) A probabilistic 311 model, which in each trial deploys WADD with probability 312313 p and *TTB* with probability (1-p). While this model assumes a trembling-hand error (as before), p provides a 314continuous measure of the degree of WADD use. (ii) A 315316 model that is like (i) with the exception that the WADD errors are not due to a trembling hand assumption, but 317 rather are assumed to reflect Gaussian fluctuations in the 318 319WADD estimation (with zero mean and whose SD is a new 320 model parameter); we still have a trembling hand parame-321 ter for errors of the *TTB* heuristic (see Lee & Newell, 2011;



Fig. 3 Averaged standardized regression coefficients of: *left* ($\Delta WA - difficulty$) – for graphic purposes we plotted *the negatives of the difficulty-coefficients*, and *right* (*Tie**No Tie*) – whether there was a tie on the most important dimension, separately for participants classified as users of *WADD* and *TTB* strategies. Error bars represent standard errors

Scheibehenne, Rieskamp, & Wagenmakers, 2013; for sim-322 ilar approaches to mixture models in decision-making). 323 (iii) A fully compensatory model, whose weights are char-324acterized by a single parameter, α , based on normalized 325 W^{α}_{i} (where W_i are the normative weights (e.g., 4,3,2,1); 326 note that $\alpha > 1$ results in an over-weighting of the high 327 weights and under-weighting of the low weights, as in 328 some version of the PCS; Glöckner et al., 2014). For each 329 model, the parameters were fitted based on the probability 330 of the data given the model (see Supplementary Material). 331The results are summarized at the group level in Table 4 332 (see Supplementary Material for individual participants' 333 classifications). 334

We observe a clear picture. The single-strategy trembling-335 hand models provide the worst fit, followed by the compen-336 satory α -weight model, and then by the probabilistic strategy 337 mixture WADD/TTB model. The best model by far is the mix-338 ture model with Gaussian WADD errors. Importantly, the pro-339 portion of WADD use in this model shows high consistency 340 among the participants across the number of attributes (see 341 Suppl.). Furthermore, we also find high correlations between 342 the proportion of WADD use in the probabilistic model of 343 individual subjects and subjective α -weights (all |r|s >.75; 344p<.001; see Supplementary Material). 345



Fig. 2 Subjective weights for jobs with three (left), four (middle), and five (right) attributes, classified by strategy used. Error bars correspond to standard errors

t4.1 Table 4 Akaike Information Criterion (AIC) table ^a for models of strategy choice						
t4.2	Model	Pure TTB	Pure WADD	Binary Mixture Model (TTB + WADD)	Gaussian mixture model (TTB + WADD)	α-weight model
t4.3	Three attributes	3,941	3,135	2,566	2,283	2,652
t4.4	Four attributes	4,413	3,914	3,028	2,681	3,241
t4.5	Five attributes	4,800	4,333	3,510	3,099	3,672

Note that AIC differences higher than 10 are considered decisive evidence (bold values indicate the best fits)

a The same conclusions are obtained with Bayesian Information Criterion (see Tables S8-S10 in Supplementary Material)

346 **Discussion**

In this study, we asked whether participants can rapidly 347 carry out a complex weighted-averaging task. We used a 348 349 job-interview framing and provided the participants with accuracy feedback. The number of attributes varied from 350351three to five, a range exceeding the capacity of online 352analytical computations for speedy decisions. The results were surprising. First, the decision times (Mean-RT ~1.5 353s, which includes the visual encoding and the motor re-354355 sponse) were much faster than the maximum allotted time, 356 indicating reliance on intuitive gist-perceptions or heuristic rules (Saunders & Buehner, 2013). Second, despite the 357 short RTs, the accuracy exceeded the bound that could be 358 359obtained on the basis of (error-less) non-compensatory 360 strategies, such as TTB. Third, we found a negative correlation between accuracy and decision-time, consistent 361 362 with evidence integration models, such as those based 363 on the Decision-Field-Theory (Roe et al., 2001), the drift-diffusion model (Krajbich, Armel, & Rangel, 2010) 364365 or PCS (Glöckner et al., 2014). These results are consistent with those obtained by Glöckner and Betsch (2008, 366 367 2012) in a multi-cue probabilistic inference task, and with 368 their proposal of an automatic compensatory mechanism.

369 We examined two simplifying heuristics: One that (TTB) is 370 non-compensatory, while the other (EQW-TTB) neglects the 371importance of the decision attributes. While the group-level 372 performance exceeded the accuracy bound achievable from an 373 error-free TTB heuristic, at the individual participants' level we 374 found a certain amount of variability. The simplified 375(dichotomous) classification showed that, while most participants relied on compensatory strategies, about 30% relied on 376 377 the TTB heuristic. These participants were characterized by a 378peaked decision-weight pattern that overestimates the most 379 important attribute (Fig. 2), by reduced task accuracy (without 380 a Speed-Accuracy trade-off). TTB-users were also slower in trials with a tie on the most important dimension (Fig. 3, right 381panel). Unlike TTB users, most participants appeared to de-382ploy a compensatory strategy that is likely to involve a noisy 383 384estimation of the weighted average (WADD; see also Glöckner 385& Betsch, 2008). The more refined (mixture) classifications 386 indicate a continuum for participants' probability of deploying a compensatory *WADD* strategy in each trial, ranging from a 387 minimum of .23 to a maximum of 1. 388

We suggest that the presence of variability in decision strat-389 egies across the group reflects two potential ways of dealing 390 with time pressure and information overload in decision mak-391 ing. The non-compensatory TTB heuristic is a lexicographic 392 strategy that applies rules sequentially and neglects much of 393 the information. Automatic and compensatory (WADD) strat-394egies offer an alternative way to deal with information over-395 load. Instead of "calculating" the weighted average, these par-396 ticipants appear to carry out an "approximate" (noisy), but 397 holistic estimation of it, consistent with an affective/intuitive 398 decision mode (Kahneman, 2003). In particular, intuitive/ 399 holistic averaging is consistent with Kahneman's suggestion 400 that intuitive processes are holistic in nature (see also 401 Glöckner and Betsch, 2008) and are at the interface of percep-402 tion and cognition (Kahneman, 2003). This suggestion was 403 also supported by recent empirical results showing dissocia-404 tions between intuitive and analytical averaging based on load 405manipulations (Rusou et al., 2017). 406

A potential mechanism to perform noisy weighted averag-407 ing estimations is Glöckner and colleagues' PCS model 408 (Glöckner, Hilbig & Jekel, 2014). According to this model, 409 the weighted average is computed in a neural network, which 410multiplies a values-vector with an importance-weights matrix. 411 As our task involves some practice, the assumption that the 412decision mechanism includes learned weights (reflecting the 413 attributes' importance) is not implausible.² Alternatively, the 414 mechanism of weighted averaging could be mediated by a 415population code model (Brezis et al., 2016; Brezis et al., 4162015), which operates using numerosity detectors (Dehaene, 417Molko, Cohen & Wilson, 2004; Piazza, Izard, Pinel, Le 418 Bihan, & Dehaene, 2004). Future research is needed to probe 419

² This does not require to endorse all the assumptions of the *PCS* model, such as RT being based on convergence to asymptotic activation; an alternative assumption is an integration to boundary. The property of *PCS* that is important to our results is the parallel integration of values from all attributes. A somewhat similar approach is the accumulator model proposed by Lee and Cummins (2004), according to which the integrated values are subject to a response-boundary. This model, however, assumes that the values are integrated sequentially (in order of importance) and accounts for *TTB* use for low boundary values. Since in our data *TTB* users were not faster than *WADD* users, we support the parallel rather than the sequential integration of values.

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