

**Usher Lab**

Decisions

Cognition

Neural Computation



TEL AVIV אוניברסיטת  
UNIVERSITY תל אביב

# The cognition/metacognition tradeoff

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# Choice & Confidence & Confidence-resolution (*metacognitive*)



- **Task: predict who will win in elections**
- **Rate your confidence on a 1-6 scale**

1	2	3	4	5	6
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## Confidence resolution:

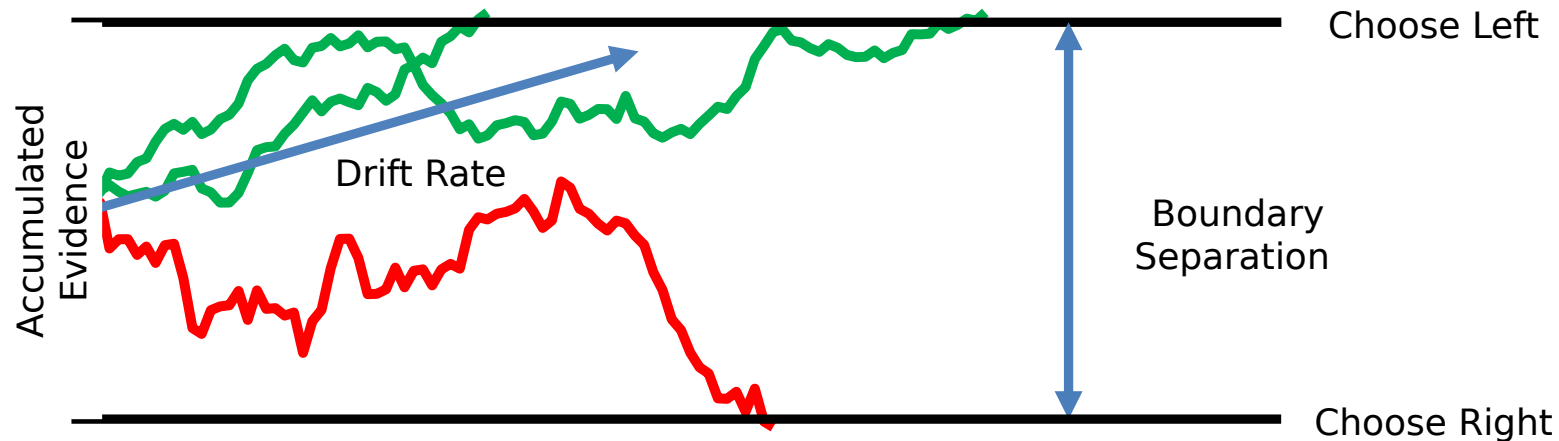
confidence (correct) – Confidence (incorrect) > 0

(Other measures: Gamma-correlation; Type-2 AUROC)

# Integration to boundary

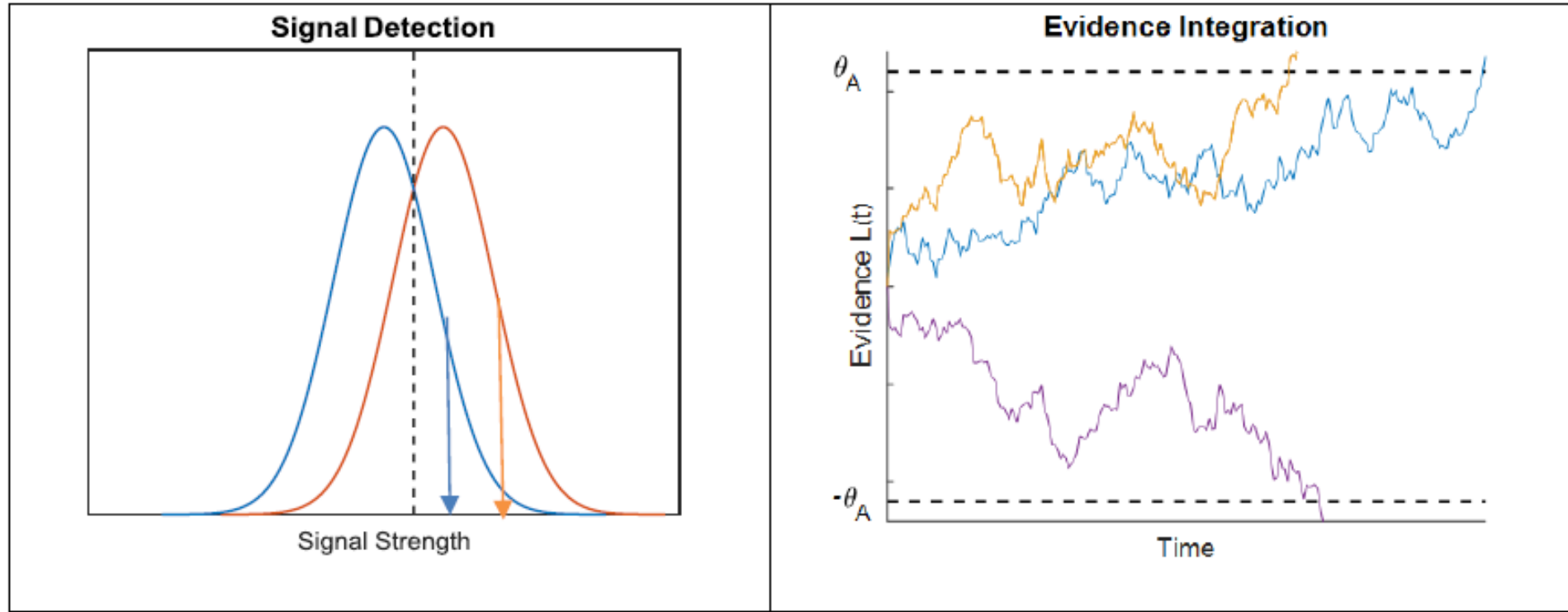
- *Normative mechanism for self-terminated decisions with stochastic evidence*

**Normative Model – SPRT: Fastest response-time for a given accuracy rate (Wald, 1947)**



- Boundary corresponds to posterior probability
- Confidence ~ subjective likelihood of being correct ~ constant
- By integrating to boundary we reduce variability in evidence that can signal accuracy and thus reduces *confidence-resolution*

# Confidence resolution in SD model VS. integration to boundary



Signal detection with *exogenous determined stimuli* (*interrogation*)

- **Distance from boundary signals confidence**
- **Confidence resolution > 0**

- Use RT as confidence indicator (Conf. negatively correlated with RT):
  - Use post-decision information (or WM)

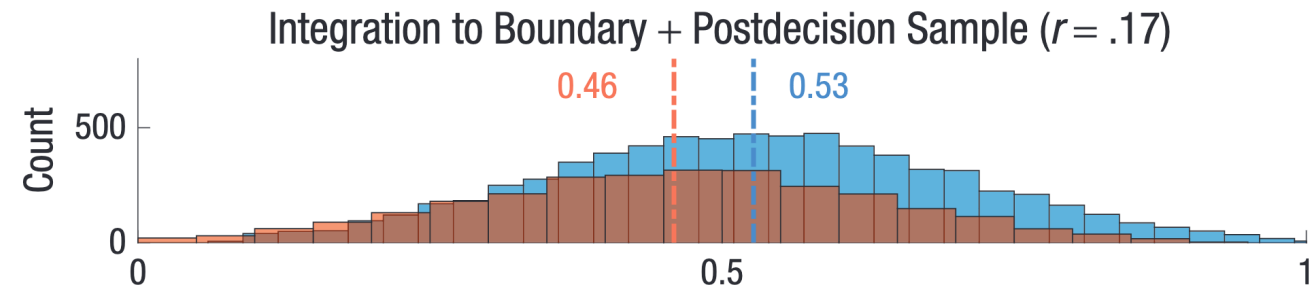
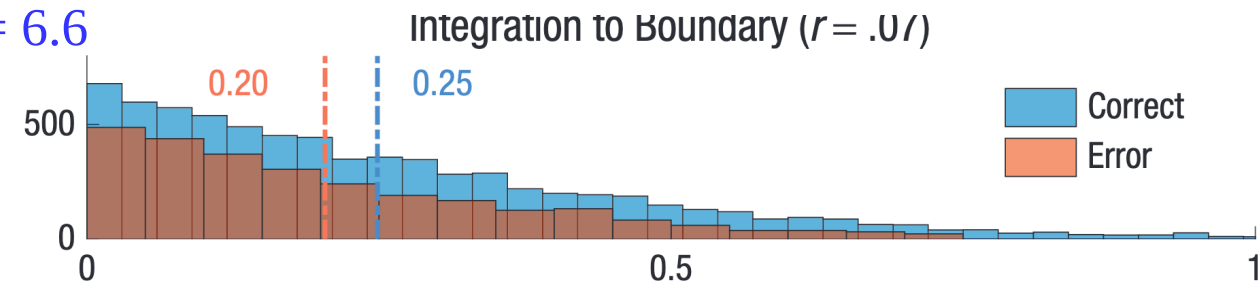
Integrated evidence for *endogenous determined stimuli* (*free choice/sampling*)

- **Decisions triggered by the same amount of evidence; Confidence resolution = 0**

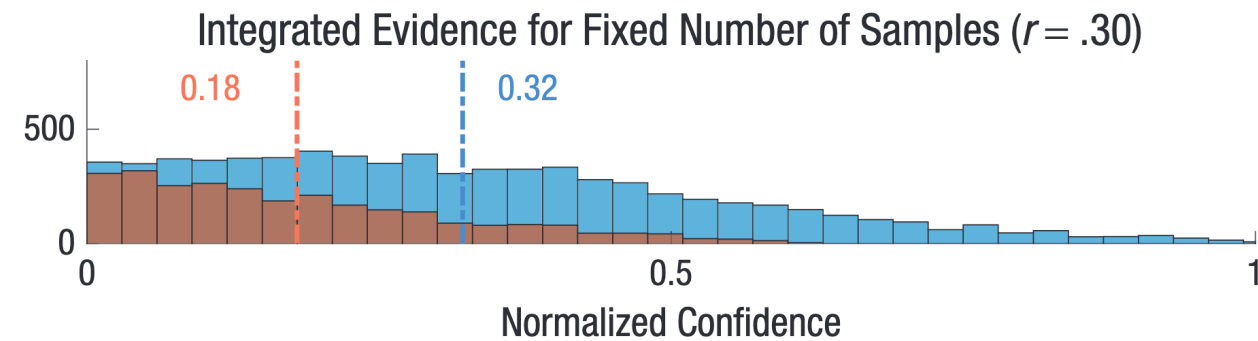
# Confidence resolution: i) Free response (**Last sample**), ii) Interrogation (SD)

Values sampled from :  $X \sim N(52, 15)$  and  $Y \sim N(48, 15)$

**Integration to boundary:** Accuracy 72%; Mean-RT = 6.6



**Fixed-time integration:** Accuracy = 72%; Mean-RT = 10



**Fig. 3.** Confidence distributions for three models of choice and confidence. For each model,

Does integration to boundary  
have a cost in confidence resolution?

# Study Goals



- Comparing confidence resolution between the interrogation and FR sessions with equal number of samples
- Comparing confidence predictors between the two sessions

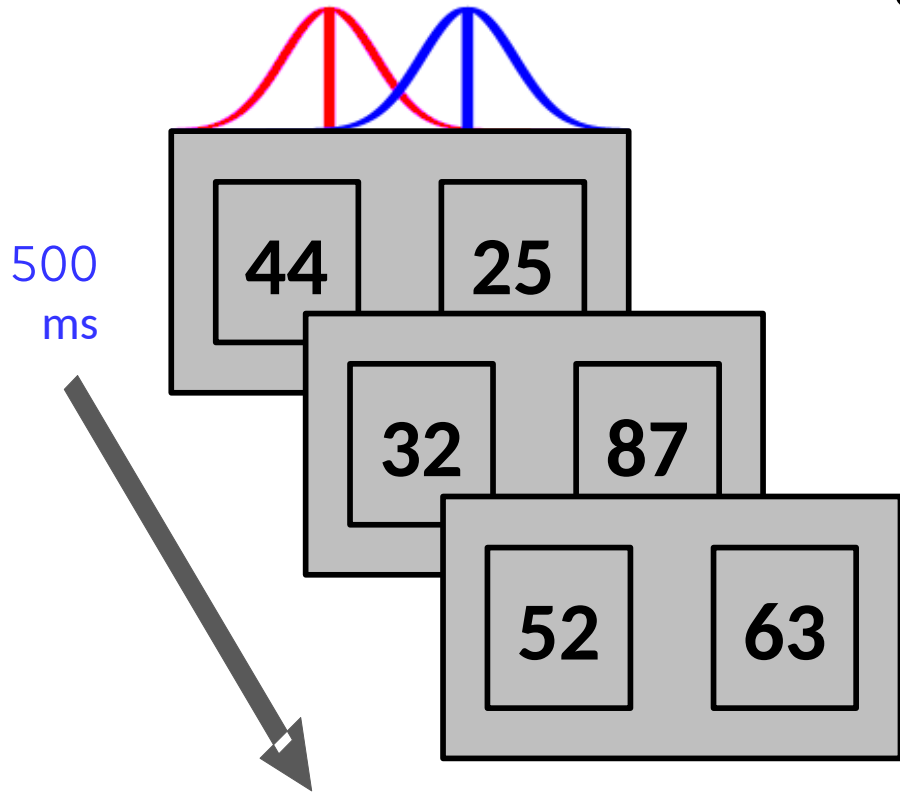
# Study Goals



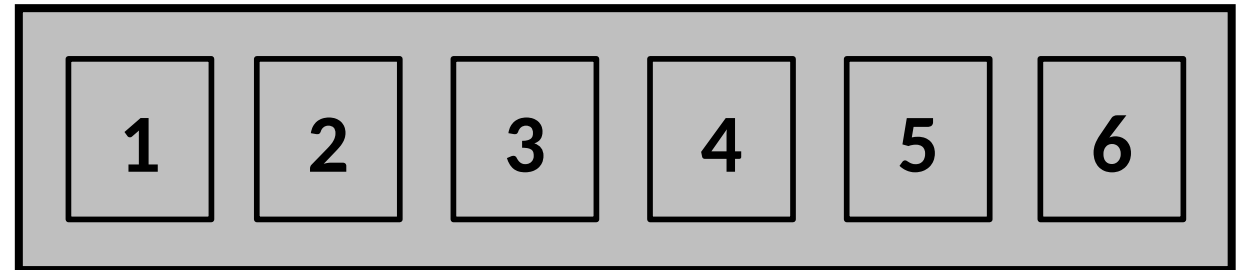
- Comparing confidence resolution between the interrogation and FR sessions with equal number of samples
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# Value integration choice task



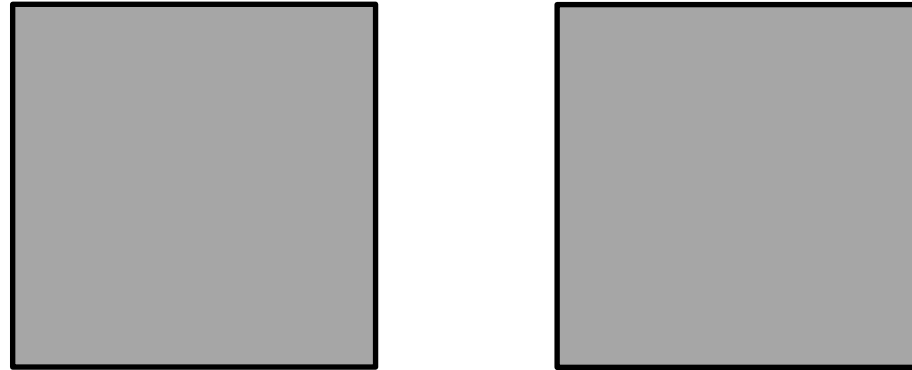
- Two sequences of numerical values
- Samples were drawn from 2 Gaussians
- Task: choose the sequence with the higher mean
- Rate your confidence on a 1-6 scale
- Session 1 = Free response paradigm
- Session 2 = Interrogation paradigm



- For each S, session-2 presents trials with the same number of frames & sampled from the same payoff distributions as in session-1

# Value integration choice task

(Glickman & Usher, 2019; Glickman et al., 2018; Tsetsos et al., 2012)



Which sequence was drawn from a ?  
distribution with a higher mean

66

38

67

56

**37**

**47**

51

67

33

50

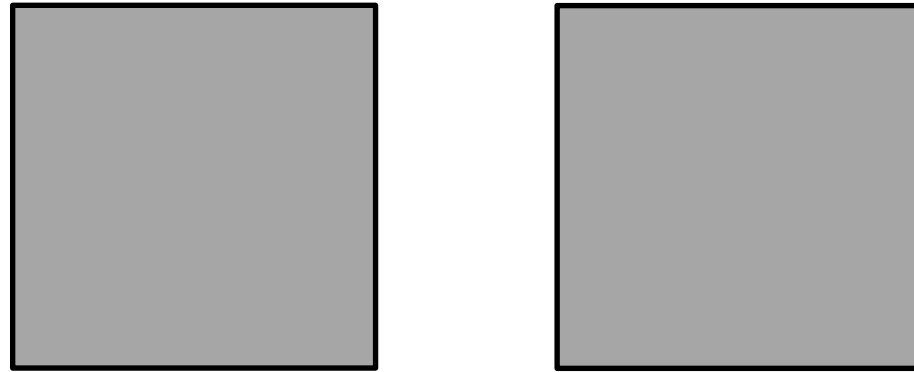
50

58

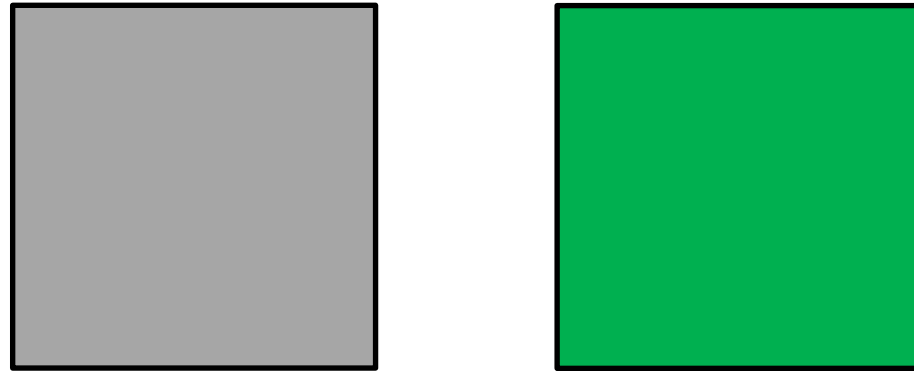


**73**

**67**



**Decision:** Right or left  
**Confidence rate:** On a 1-6 scale



**Decision:** Right (Correct)

**Free response:** Decision terminates the trial

**Interrogation:** Fixed number of samples  
(matched trial by trial)

## 2 within-S experiments

- Exp. 1 (N=17)
- Exp. 2 (Preregistered replication; N=35)

Is there a cost in confidence resolution from self-terminated (free choice) compared to exp. terminated (interrogation)?

# Results: accuracy and conf-resolution

## Experiment 1

	Accuracy	Conf-resolution	Gamma correlation	Type 2 AUROC
Free-response	81.	87.	51.	67.
Interrogation	81.	1.01	58.	70.
<i>t</i> -test	$t(16)=0.44, p = .66$	$t(16)=2.33, p = .03$	$t(16)=1.83, p = .08$	$t(16)=2.11, p = .05$

## Experiment 2

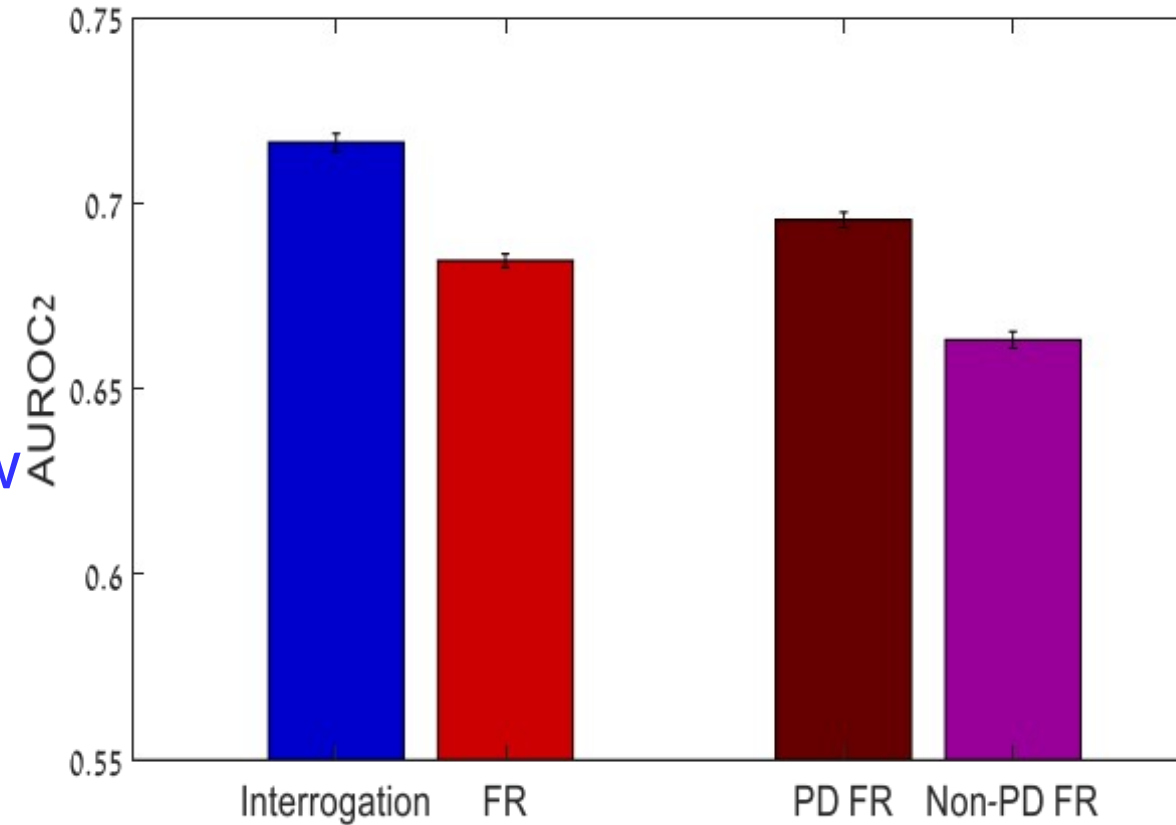
	Accuracy	Conf-resolution	Gamma correlation	Type 2 AUROC
Free response	79.	84.	49.	67.
Interrogation	83.	1.1	59.	0.72
	$t(34)=5.7, p<.001$	$F(1,1)=2.7, p =.1$	$F(1,1)=4.9, p =.03$	$F(1,1)=5, p = .03$

***t*-test**

**Ancova**

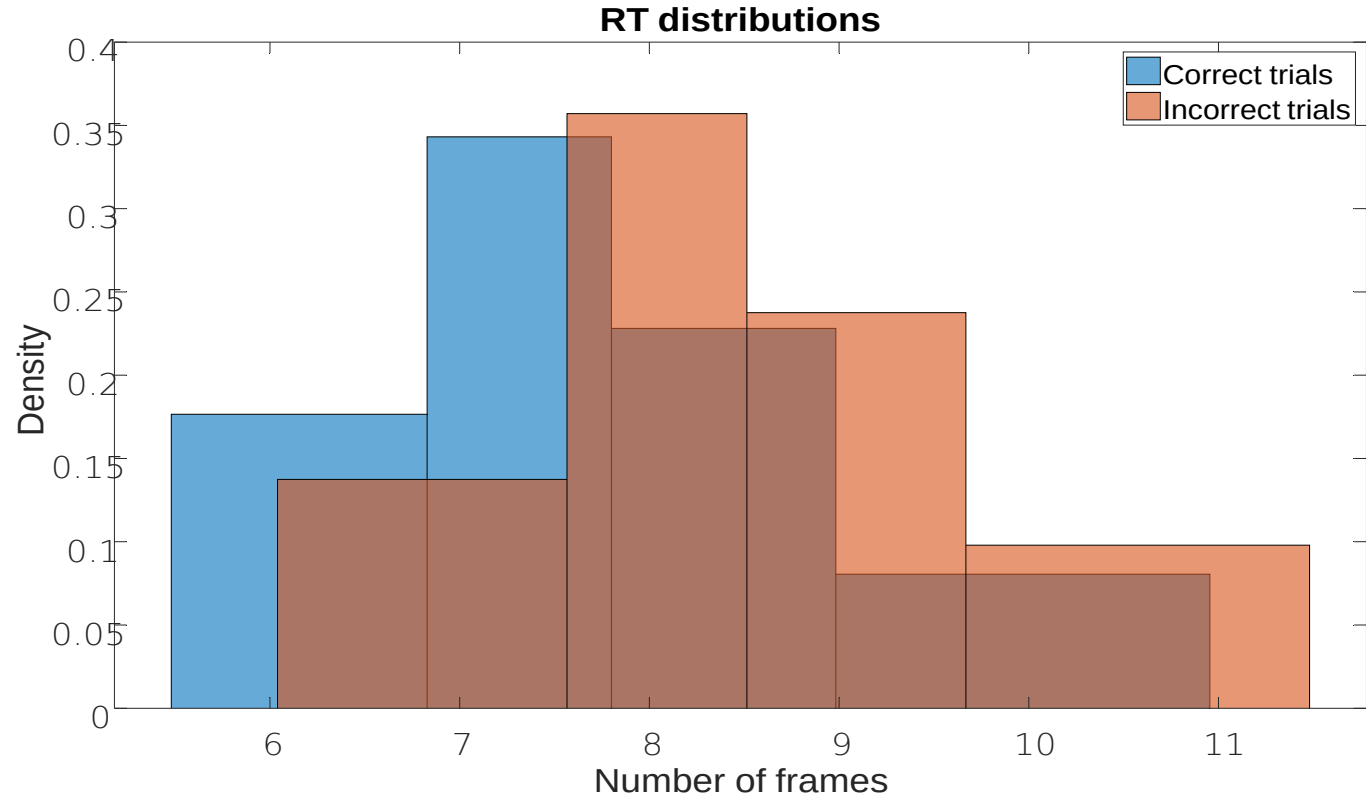
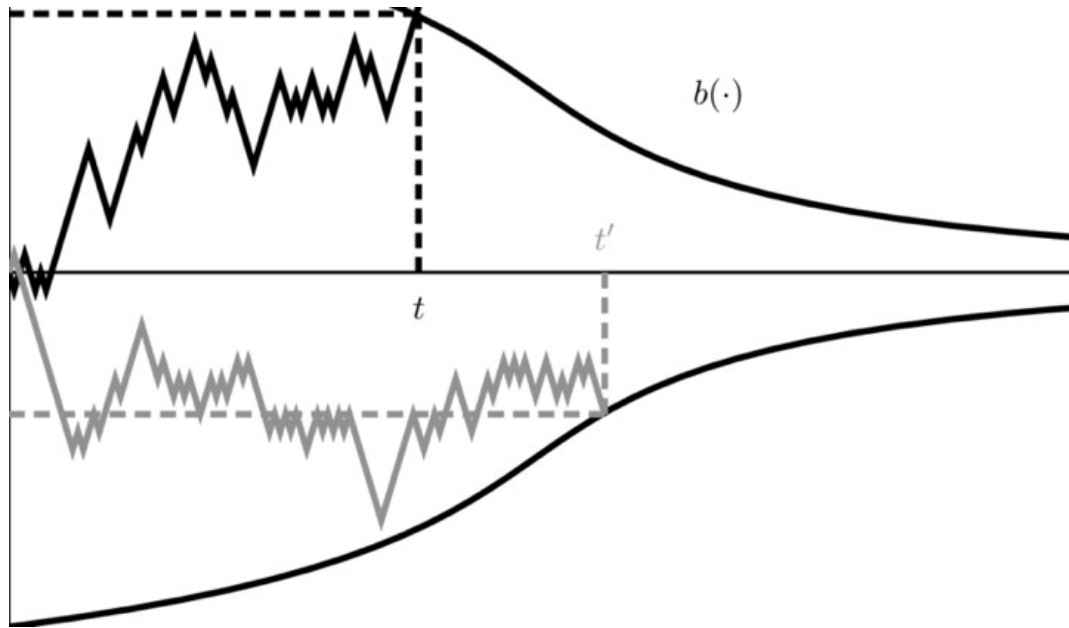
# ? What contributes to confidence-resolution in free response

- **1) Post-decision mechanism** (Pleskac & Busemeyer, 2010): fast RT (<250 ms from last frame) correspond to stimuli in which choice was determined before last frame:
- Separate free response trials into fast/slow ones (relative to last event)

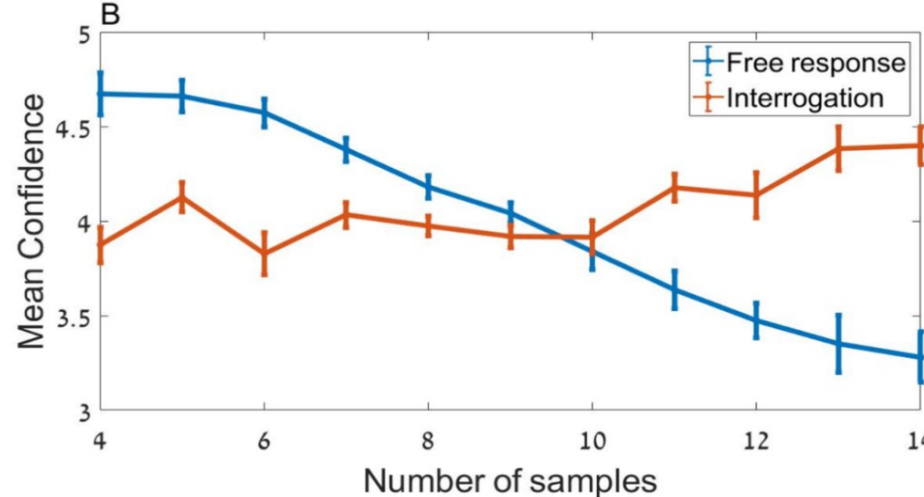
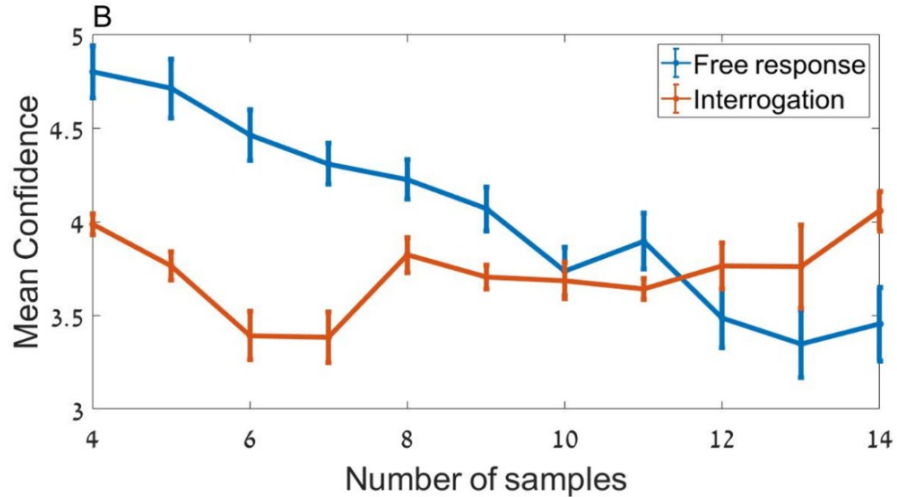
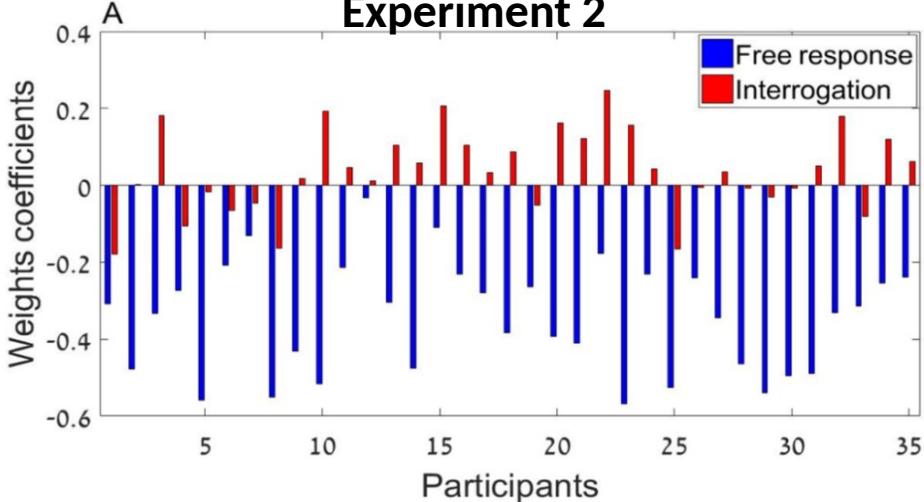
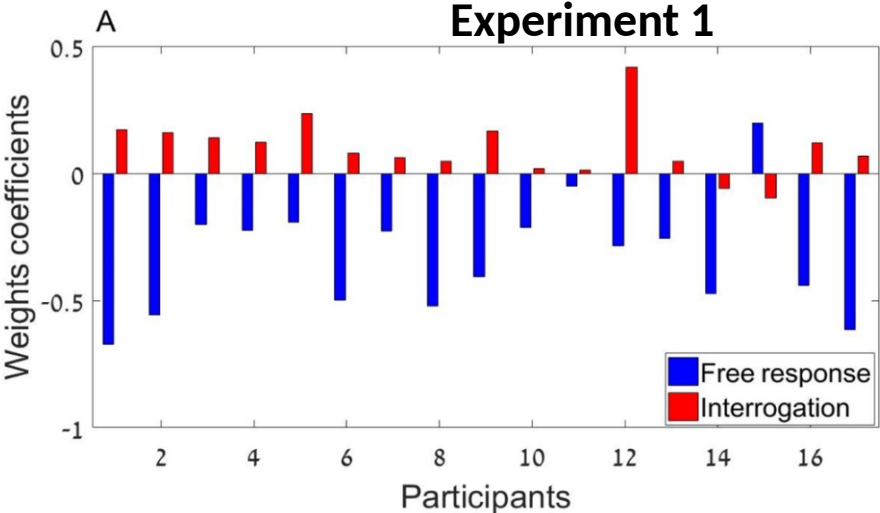


# CONF-resolution in free-choice: 2) RT

RT for integration to collapsing boundary: if correct choices are faster than incorrect choices



# Confidence-RT correlations (free choice vs interrogation)

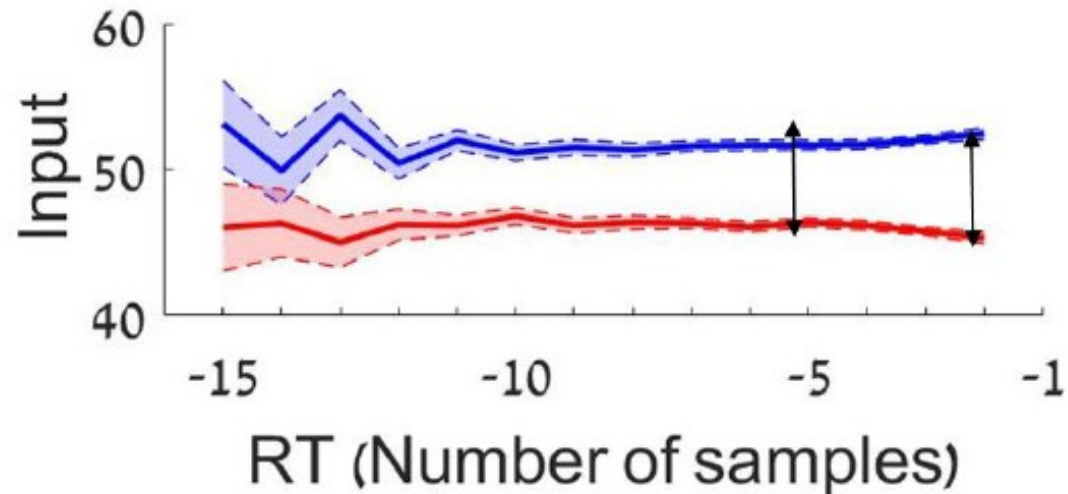
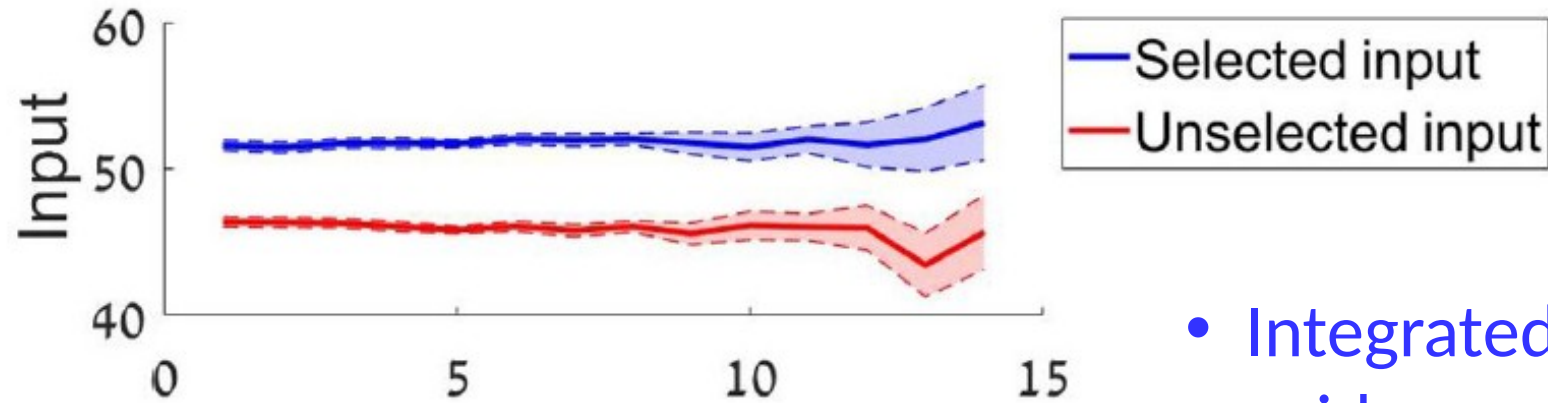




# Computational models for FR choice (model selection)

Vickers' Accumulator model	Diffusion model Collapsed	Diffusion model Fixed	
1 (967)	34 (801)	0 (1000)	Winners Frequency (Group BIC)

# Computational models for interrogation choice



- Integrated evidence/Leaky integrated evidence
- No implicit boundary (REVERSE CORRELATION)

# Computational models for confidence in FR

## Several models to predict confidence:

- Accumulated evidence =
- Leaky accumulated evidence =  $\lambda^{n-i}$
- RT (number of samples in each trial)
- Last item evidence =
- Last item evidence-1=
- Stop boundary point (correlated with RT)
- Split evidence=

# Computational models for confidence

## Free response session

Model	BIC	R	LL*(2-)
<b>Last Item Evidence_Rest Evidence_RT</b>	<b>346.50</b>	<b>0.57</b>	<b>326.88</b>
Last Item Evidence_RT	352.42	0.53	337.71
Split Last Item_RT	354.97	0.53	335.35
<b>Last Item Evidence_Stopping Point Boundary</b>	<b>355.14</b>	<b>0.51</b>	<b>340.42</b>
Accumulated Evidence_RT	355.30	0.51	340.59
Last Item Evidence_Stopping Point Boundary_RT	355.70	0.53	336.08
Leaky Integrated Evidence	356.86	0.51	342.00
Split Last Item_Stopping Point	357.64	0.52	338.02
Last Item Evidence_Rest Evidence	360.60	0.48	345.89
Last Item Evidence_Last Item Evidence-1_Rest	361.79	0.50	342.17
Accumulated Evidence	368.16	0.41	358.35
Selected Samples_Unselected Samples	374.37	0.50	340.04

# Computational models for confidence

## Interrogation session

Model	BIC	R	LL*(2-)
<b>AccumulatedEvidence</b>	<b>357.65</b>	0.48	347.84
<b>LeakyIntegratedEvidence</b>	358.3	<b>0.50</b>	343.59
LastItemEvidence_RestEvidence	359.32	0.49	344.6
AccumulatedEvidence_RT	359.86	0.49	345.14
LastItemEvidence_RestEvidence_RT	361.84	0.50	342.23
LastItemEvidence_LastItemEvidence-1_RestEvidence	362.42	0.50	342.81
LastItemEvidence_LastItemEvidence-1_RestEvidence_RT	361.13	0.50	340.61
LastItemEvidence_RT	389.41	0.25	374.70
SelectedSamples_UnselectedSamples	392.82	0.37	358.50
SplitLastItem_RT	393.08	0.25	373.47

# Summary

- Integration to boundary is optimal for choice
- This comes with a cost in confidence-resolution: integrating to boundary reduces variability in relevant evidence that can signal posterior probability
- Some confidence resolution can be achieved by post-decision mechanism or by using collapsing boundaries (if corrects are faster than incorrects)
- The confidence mechanism differs in integration-to boundary (*RT & post-decision*) vs fix number of samples (*SD based on total evidence*)

Rosenbaum D, Glickman M, Fleming SM & Usher M (2022).

The Cognition/Metacognition Trade-Off. ***Psychological Science***.

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